

رابعة اتصالات

مقرر OPTICS

part (9)

Sec (9)

In last section :

$$I(z) = I_0 e^{\gamma z}$$

irradiance at z

Input irradiance



Where:

$$\gamma = \frac{B P(\nu) h \nu}{v} \left(P_e - P_{abs} \right) \rightarrow \textcircled{1}$$

$$B = \frac{v^3}{8 \pi h^2 f^3}$$

$$P(\nu) = \frac{(2 m r)^{3/2}}{\pi \hbar^2} (h \nu - E_g)^{1/2}$$

$$I(z) > I_0 \rightarrow \text{When } \gamma \rightarrow +ve \Rightarrow \gamma \rightarrow \text{Gain}$$

$$I(z) < I_0 \rightarrow \text{When } \gamma \rightarrow -ve \Rightarrow \gamma \rightarrow \text{Attenuation}$$

↳ Condition of Amplification Gain:

$$\gamma \rightarrow +ve \quad (\text{In eqn. } \textcircled{1})$$

$$\text{when } \textcircled{1} P_e > P_{abs}$$

$$\textcircled{2} P(\nu) \rightarrow +ve$$

$$\text{when } h \nu > E_g$$

↳ $P_e > P_{abs}$ In Quasiequilibrium :

$$P_e = f(E_2) [1 - f(E_1)] = \frac{1}{1 + e^{(E_1 - E_F)/kT}} \left[\frac{e^{(E_2 - E_F)/kT}}{1 + e^{(E_1 - E_F)/kT}} \right]$$

$$P_{abs} = f(E_1) [1 - f(E_2)] = \frac{1}{1 + e^{(E_1 - E_F)/kT}} \left[\frac{e^{(E_2 - E_F)/kT}}{1 + e^{(E_2 - E_F)/kT}} \right]$$

II

$$P_e > P_{abs}$$

When
$$\frac{(E_1 - E_{FV})}{kT} > \frac{(E_2 - E_{Fc})}{kT}$$

$$E_1 - E_{FV} > E_2 - E_{Fc}$$

$$E_1 - E_2 > E_{FV} - E_{Fc}$$

or
$$E_2 - E_1 < E_{Fc} - E_{FV}$$

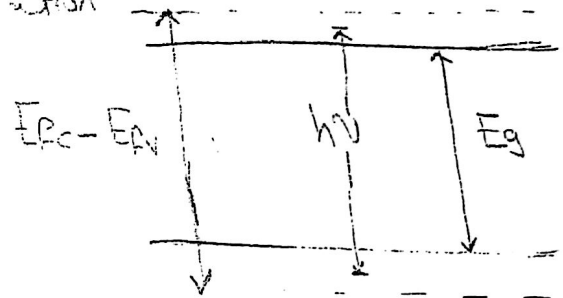
$$h\nu < E_{Fc} - E_{FV}$$

$\leftrightarrow \delta \rightarrow +ve$ when
$$E_g < h\nu < E_{Fc} - E_{FV}$$

Condition of Amplification

$$\frac{E_g}{-h} < \nu < \frac{E_{Fc} - E_{FV}}{-h}$$

$$B.W = \nu_2 - \nu_1$$



In sheet ④: Q(5)-(9) Estimate Conditions for Amp. (stimulated emission)

→ اجابتك من الصفحتين (الأولى وهذه) ..

⑦ Amplification Gain in stimulated emission

→ اجابتك كل الالجابات لي الوصول لـ δ من السكشن الـ ٢٠٢
+ ص ٢٠٢ في هذا السكشن

$$\begin{aligned} \hookrightarrow \therefore P_e - P_{abs} &= f_c(E_2) [1 - f_v(E_1)] - f_v(E_1) [1 - f_c(E_2)] \\ &= f_c(E_2) - f_c(E_2) f_v(E_1) - f_v(E_1) + f_v(E_1) f_c(E_2) \end{aligned}$$

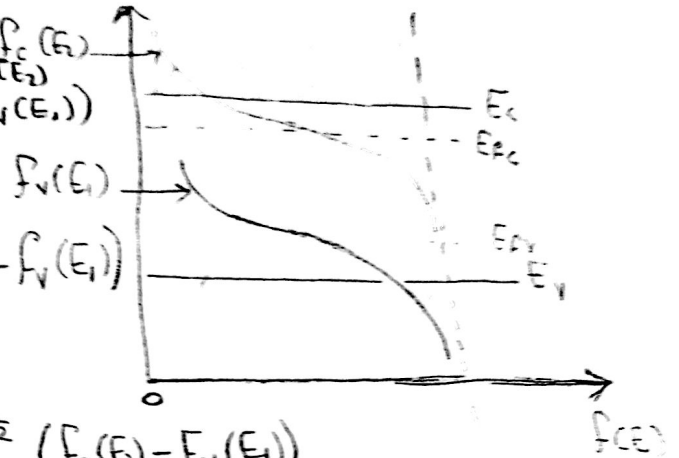
$$P_e - P_{abs} = f_c(E_2) - f_v(E_1)$$

$$\gamma = \frac{V^3}{8\pi h^3} \cdot \frac{(2m_r)^{3/2}}{\pi h^2} (h\nu - E_g)^{1/2} (f_c(E_2) - f_v(E_1))$$

$$\therefore \gamma = \frac{V^2 (2m_r)^{3/2}}{8\pi^2 \tau (\hbar)^2} (h\nu - E_g)^{1/2} (f_c(E_2) - f_v(E_1))$$

$$\gamma = \frac{(c/n)^2 \cdot (2m_r)^{3/2}}{2\tau_r (\hbar)^2} (h\nu - E_g)^{1/2} (f_c(E_2) - f_v(E_1))$$

$$\gamma = \underbrace{\frac{(c/n)^2 (2m_r)^{3/2}}{2\tau_r \hbar^2}}_{\text{Constant}} \cdot \frac{(h\nu - E_g)^{1/2}}{\nu^2} [f_c(E_2) - f_v(E_1)]$$



Case (1)

at Thermal equilibrium

$$T = 0 K$$

$$f(E) = \frac{1}{1 + e^{(E - E_f)/kT}}$$

at $E_2 > E_f$ (C.B)

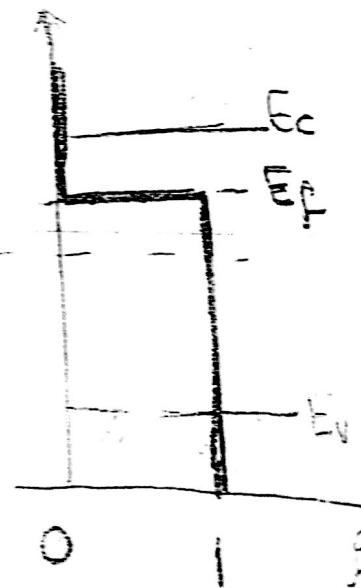
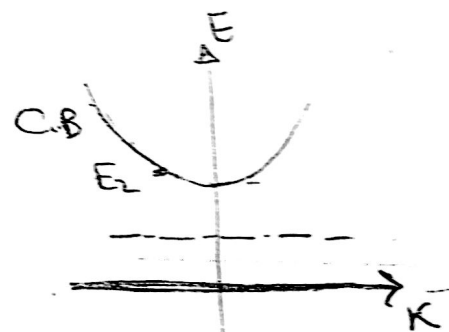
$$f(E_2) = 0$$

$E_1 < E_f$ (V.B)

$$f(E_1) = 1$$

$$\therefore f(E_2) - f(E_1) = 0 - 1 = -1$$

$\hookrightarrow \gamma \rightarrow -ve$



$$\gamma(\nu) = \text{Const.} \frac{(h\nu - E_g)^{1/2}}{\nu^2} \quad (-1)$$

→ Draw $\gamma(\nu)$ vs. ν

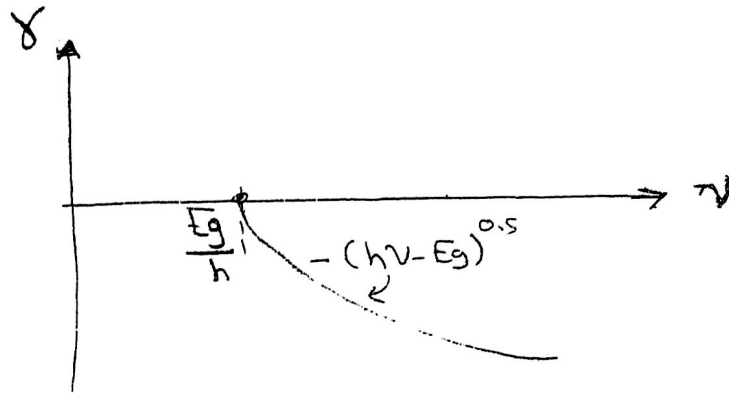
→ في الرسم محتاجا الرسم
 $-(h\nu - E_g)^{0.5}$

& $\frac{1}{\nu^2}$

→ $\Delta\nu = 10^{13} \text{ Hz}$

$\nu = 10^{14} \text{ Hz}$

→ لذلك باعتبار المتنام ثابت



Case (2) Quasi-equilibrium & $T=0K$

$$E_g \ll (E_{fc} - E_{fv}) < h\nu$$

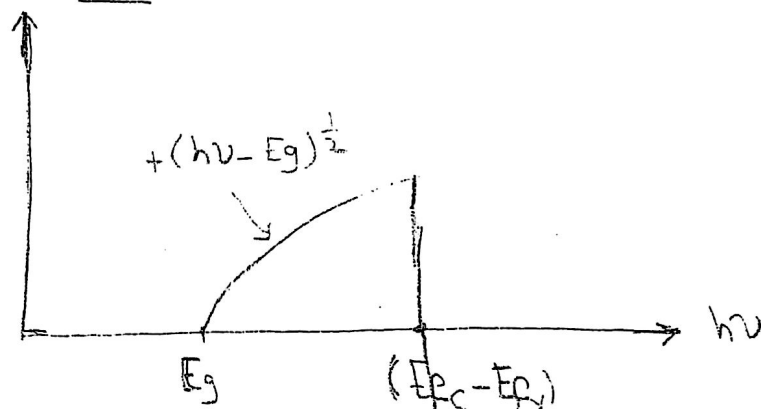
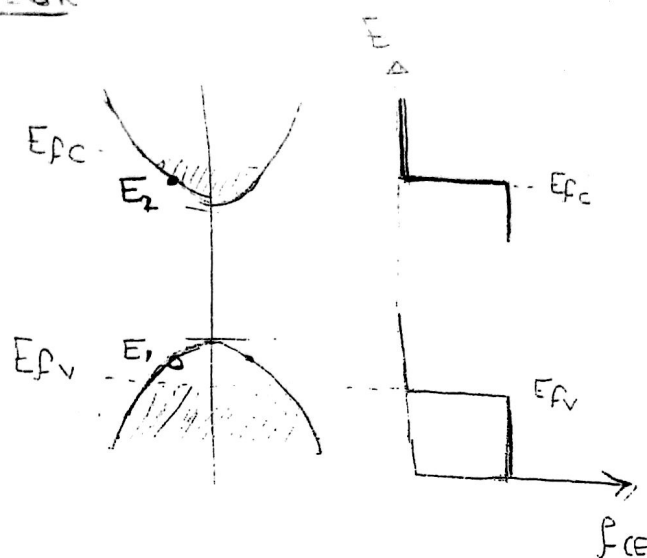
$$f(E_2) = 1$$

$$f(E_1) = 0$$

$$f(E_2) - f(E_1) = +1$$

$$\gamma \rightarrow +ve$$

Amplification Gain



When $(h\nu)$ become greater than $(E_{fc} - E_{fv}) \rightarrow \therefore \gamma \rightarrow -ve$

Quasi-equilibrium & $T=300K$

$$\text{at } h\nu < (E_{fc} - E_{fv})$$

$$\hookrightarrow \gamma \rightarrow +ve$$

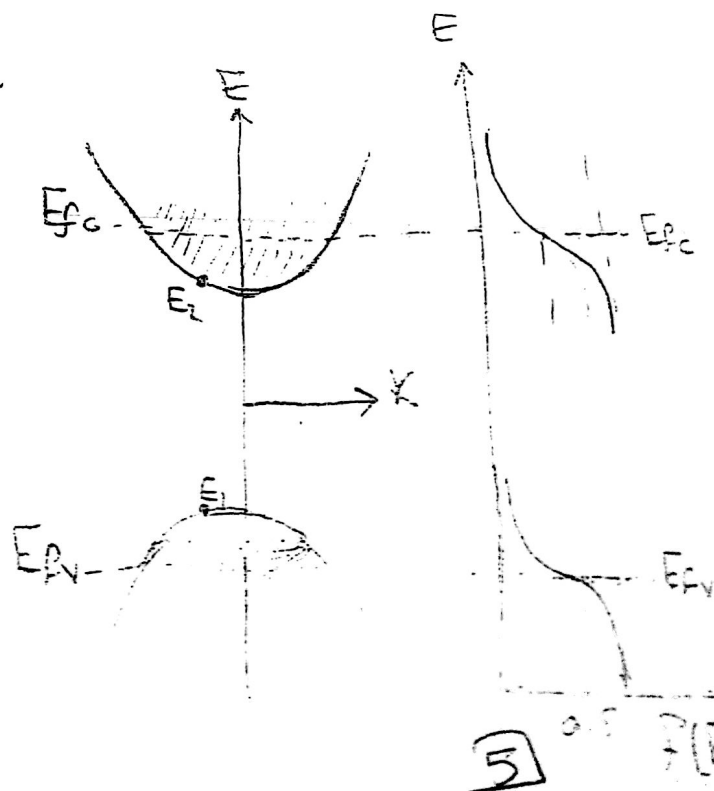
$$\text{at } h\nu = (E_{fc} - E_{fv})$$

$$f(E_2) = 0.5, f(E_1) = 0.5$$

$$\gamma = 0$$

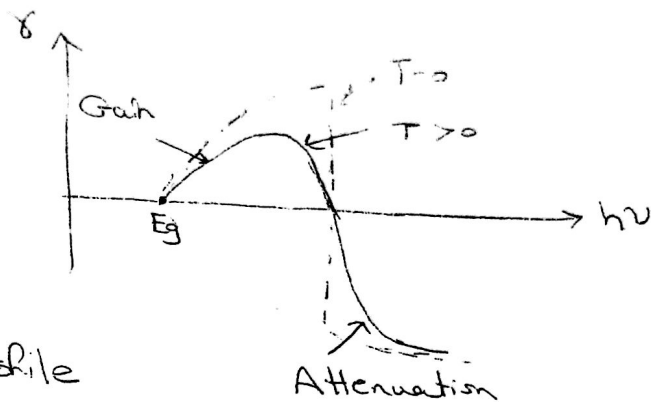
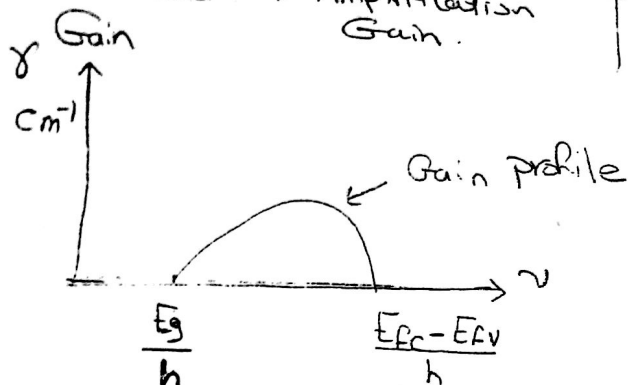
$$\text{at } h\nu > (E_{fc} - E_{fv})$$

$$\hookrightarrow \gamma = -ve$$



5 0.5 f(E)

\hookrightarrow AT $T > 0K \Rightarrow$ Amplification Gain.



$$\nu_{min} = \frac{E_g}{h}$$

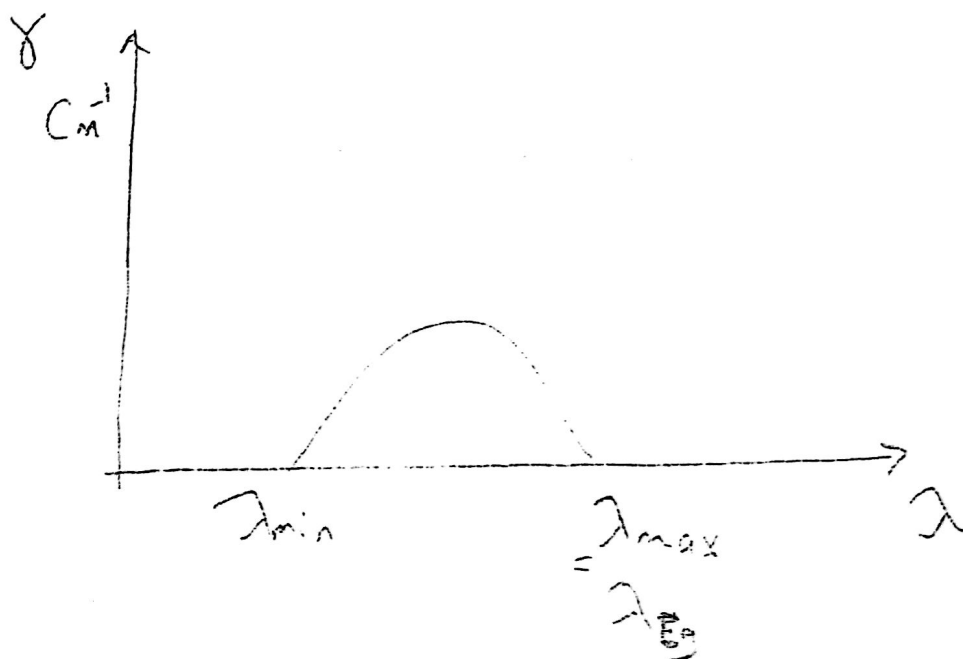
$$\frac{c}{\lambda_{max}} = \frac{E_g}{h} \Rightarrow \lambda_{max} = \frac{c \cdot h}{E_g}$$

$$\lambda_{max} = \frac{1.24}{E_g}$$

$$\lambda_{max} = \lambda_{E_g}$$

$$\nu_{max} = \frac{E_{fc} - E_{fv}}{h} \Rightarrow \frac{c}{\lambda_{min}} = \frac{E_{fc} - E_{fv}}{h}$$

$$\lambda_{min} = \frac{c \cdot h}{E_{fc} - E_{fv}} = \frac{1.24}{(E_{fc} - E_{fv})}$$



Q] Given Semiconductor amplifier $\text{In}_{0.4}\text{Ga}_{0.6}\text{As}_{0.4}\text{P}_{0.6}$ with $E_g = 1.24 \text{ eV}$, has a peak gain coeff. of 75 cm^{-1} and Amplification Bandwidth of 100 nm .

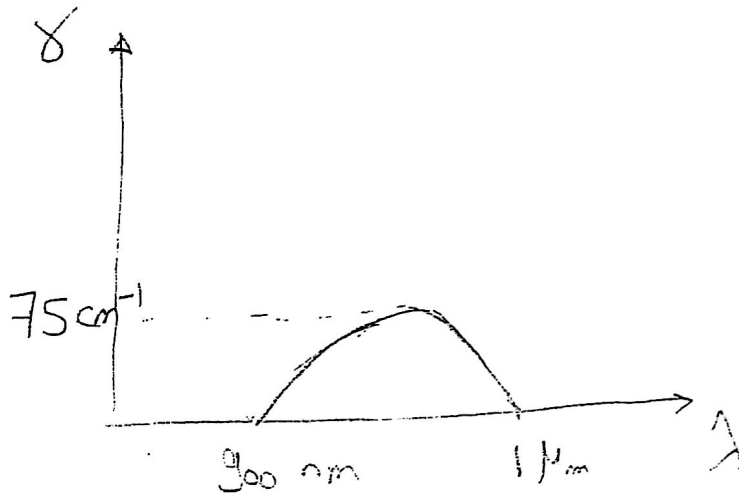
Draw qualitatively the variation of gain coeff. with wavelength in the Amp. band.

~Sol~

$$\lambda_{\text{max}} (\text{Corresponding to } E_g) = \frac{1.24}{1.24} = 1 \mu\text{m}$$

$$\therefore \text{Amp. B.W} = 100 \text{ nm} \Rightarrow \Delta\lambda = 100 \text{ nm}$$

$$\lambda_{\text{min}} = 1 \mu\text{m} - 100 \text{ nm} = 1000 \text{ nm} - 100 \text{ nm} = 900 \text{ nm}$$



Sheet ④ Q(7) Given Semiconductor Amp. $\text{In}_{0.4}\text{Ga}_{0.6}\text{As}_{0.4}\text{P}_{0.6}$ with $E_g = 1.12 \text{ eV}$ & peak gain coeff. = 60 cm^{-1} and B.W = 300 nm , draw the variation of Gain Coeff. ① with wavelength ② with Freq.

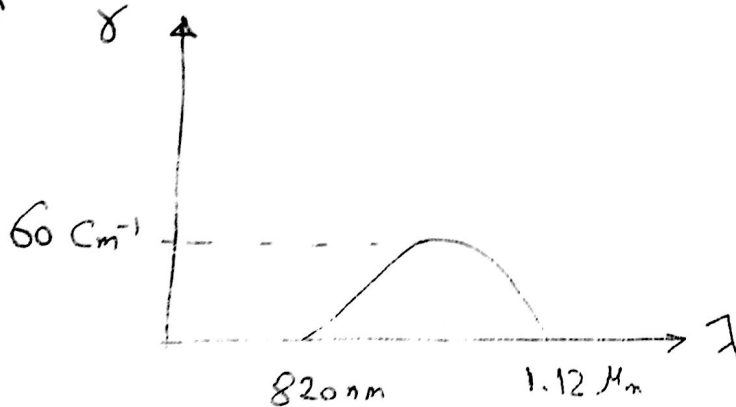
Sol

$$\textcircled{1} \lambda_{\max} = \frac{1.24}{E_g} = \frac{1.24}{1.12} = 1.12 \mu\text{m}$$

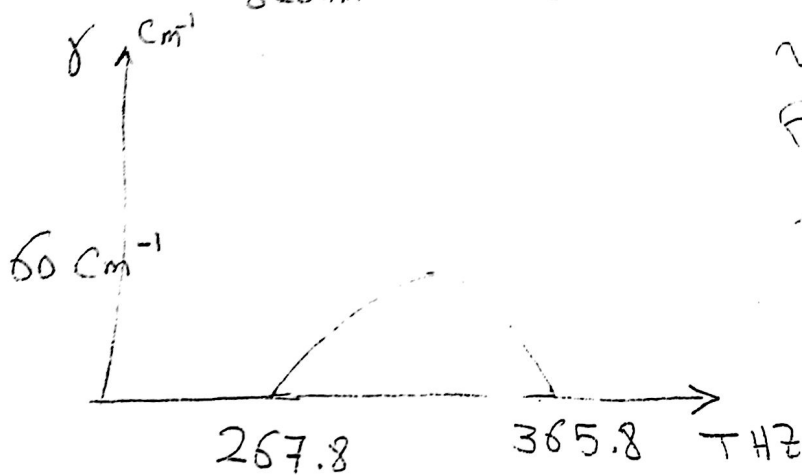
$$\text{B.W.}/_2 = 300 \text{ nm}$$

$$\lambda_{\min} = (1.12 \times 10^3) \text{ nm} - 300 = 820 \text{ nm}$$

vs. λ



vs. ν



$$\nu_{\max} = \frac{c}{\lambda_{\min}}$$

$$\nu_{\max} = 365.8 \text{ THz}$$

$$\nu_{\min} = \frac{c}{\lambda_{\max}}$$

$$\nu_{\min} = 267.8 \text{ THz}$$

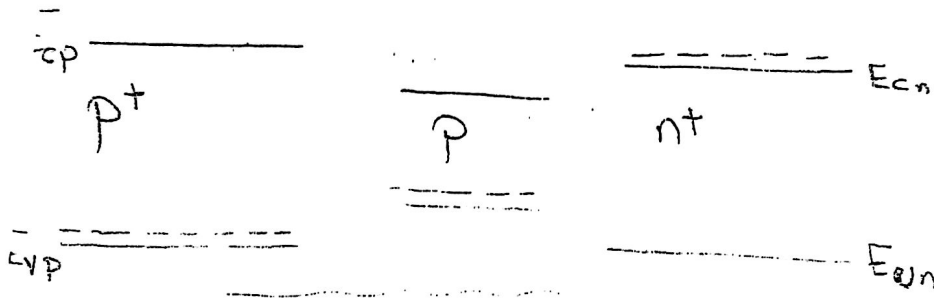
$$\Delta\nu = 98 \text{ THz}$$

(-V)

How to make $P_e > P_{abs}$? (or why we use ~~Man~~ Hetero structure
 or $(E_{fc} - E_{fv}) > E_g$ In Laser Amp ?)

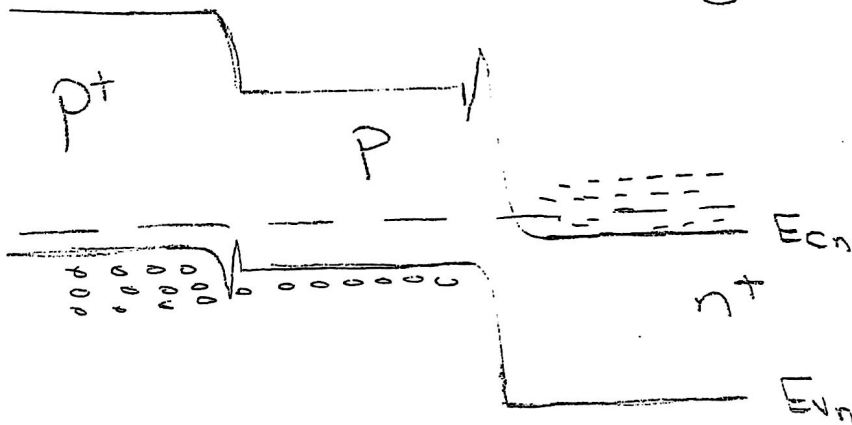
* Using Man structure Double Hetero Structure

* it is ~~necessaty~~ necessary to use highly doped material to design ~~source~~ source act as amplifier.



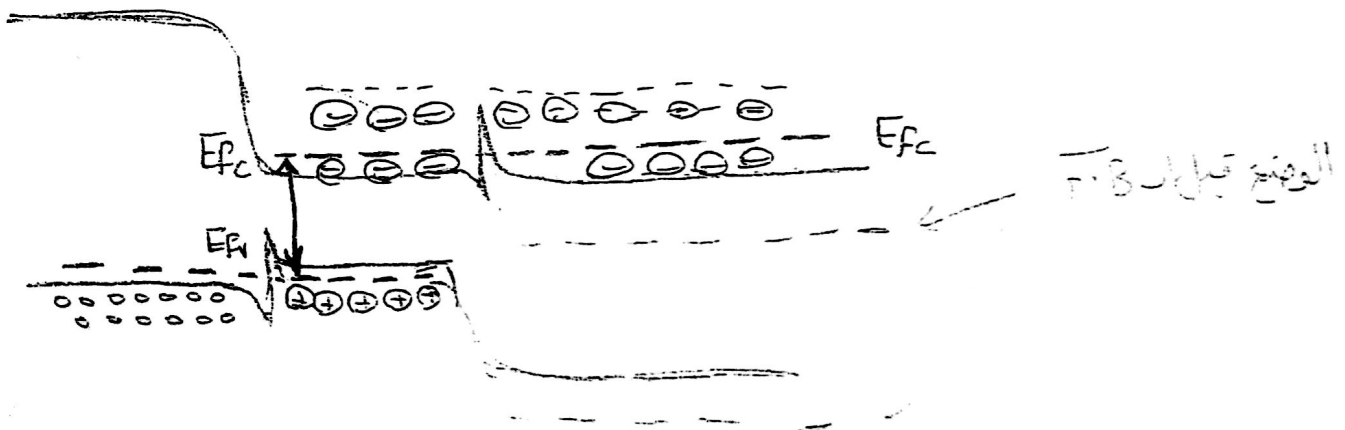
P^+	$Al_x Ga_{1-x} As$
	$Ga As P$
N^+	$Al_x Ga_{1-x} As$

① Band Diagram without Biasing

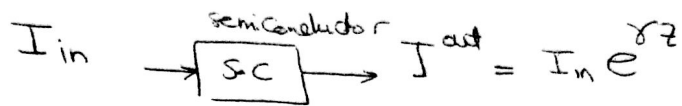


② After F.B Biasing

$$(E_{fc} - E_{fv}) > E_g$$



Absorption spectrum of Semiconductor



$$\gamma = \frac{(c/n)^2 (2m_r)^{3/2}}{2T_r \hbar^2} \cdot \frac{(\hbar\nu - E_g)^{1/2}}{\nu^2} (F_c(E_2) - F_v(E_1))$$

$\angle iR$ $\delta \rightarrow -ve$ $\gamma < 0$ when $f_c(E_2) < f_v(E_1)$

Reverse Bias ← Pn-Junction يتحقق بتوصيل

$$\gamma = \frac{(C/n)^2 (2mr)^{3/2}}{2 T_r \hbar^2} \cdot \frac{(\hbar \nu - E_g)^{1/2}}{\nu^2} \left(\underbrace{f_v(E) - f_c(E)}_{\text{+ve ans}} \right)$$

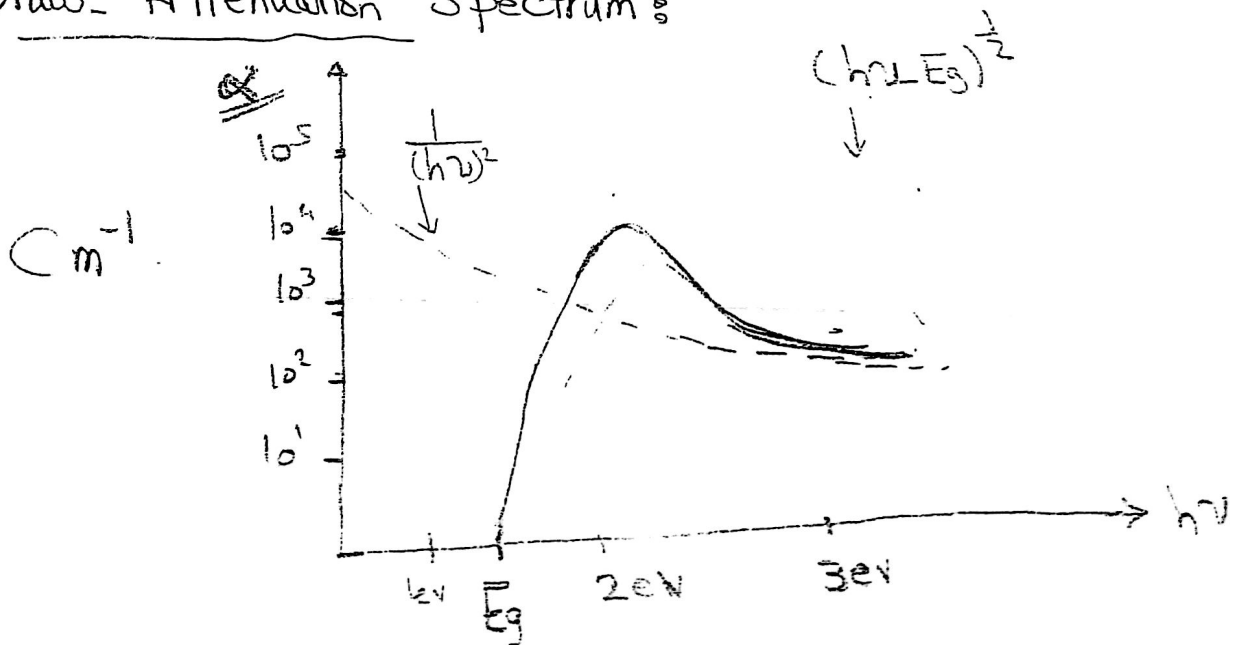
let $\gamma = -\alpha$

$$\alpha = \frac{(c/n)^2 (2m_r)^{3/2}}{2T_r \hbar^2} \cdot \frac{(\hbar\nu - E_g)^{1/2}}{\nu^2} (f_v(E_1) - f_c(E_2))$$

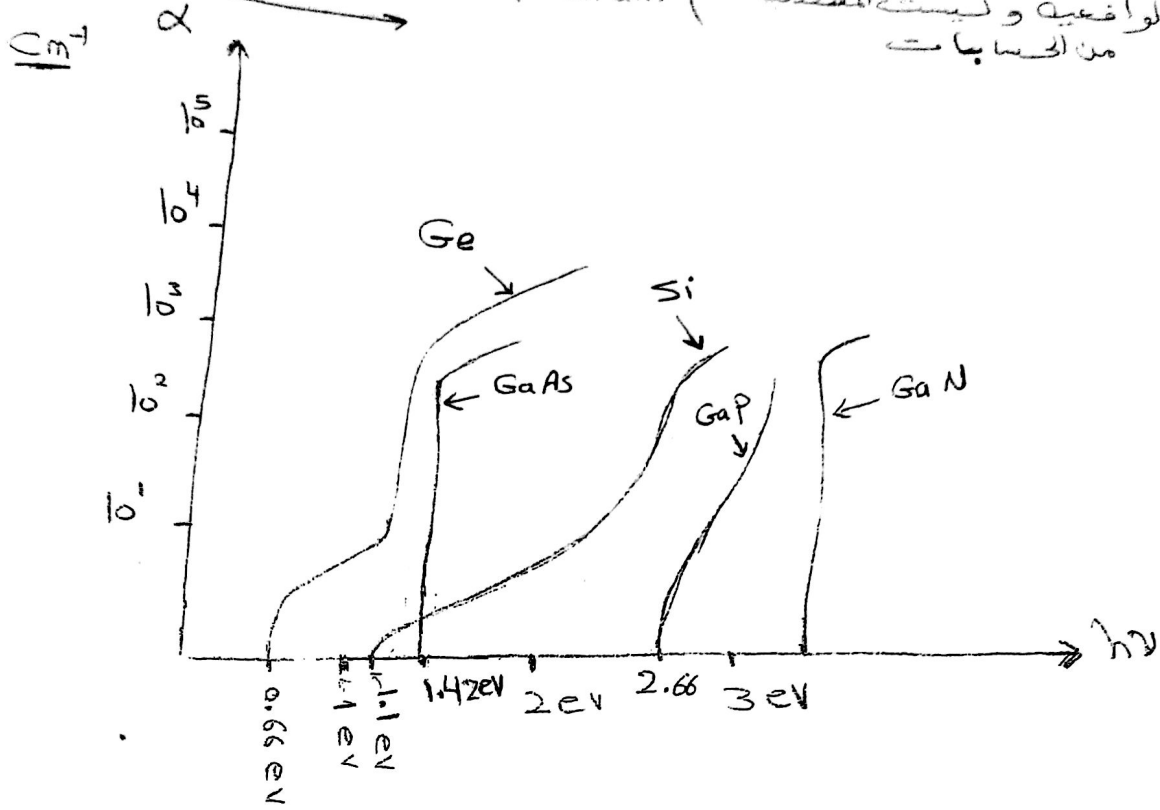
Attenuation Coeff.

$$q(\text{Absorption})$$

↳ Draw Attenuation Spectrum :



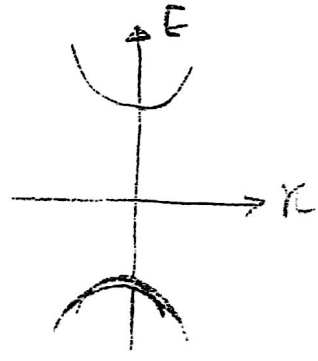
Typical Absorption Spectrum (الواقعية وليست المثالية من الحسابات)



$\left. \begin{matrix} \text{GaAs} \\ \& \text{GaN} \end{matrix} \right\} \rightarrow \text{Direct Band Gap Materials}$
 مجرد ما يكون ال (h*nu) المسقط $\leftarrow E_g =$ Absorption \leftarrow لذلك الخطوط vertical

$\left. \begin{matrix} \text{Ge} \\ \text{Si} \\ \text{GaP} \end{matrix} \right\} \rightarrow \text{Indirect Band Gap Materials}$
 أي Material لها indirect لها direct أكبر منها Band
 لذلك التغير في الأول بطيء لكن أول ما يوصل لقيمة معينة يتغير سريع

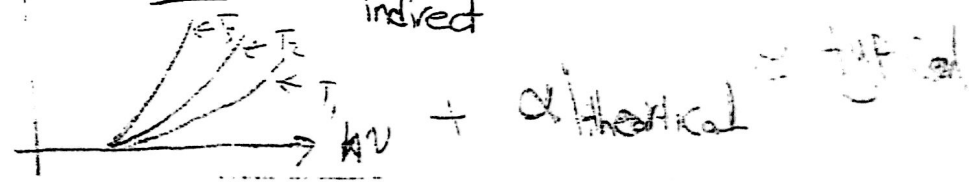
Attenuation Curve في حالة ال typical عن الحالة ال Theoretical



① لأن في ال Theoretical باستخدام ال Parabolic Approximation

لكن أي Material يكون فيها ال indirect & Direct

Note $\alpha_{\text{indirect}} = (k_0 + k_1 T) (h\nu - E_g)^2$



ده الفرض الالبييت على الحسابات

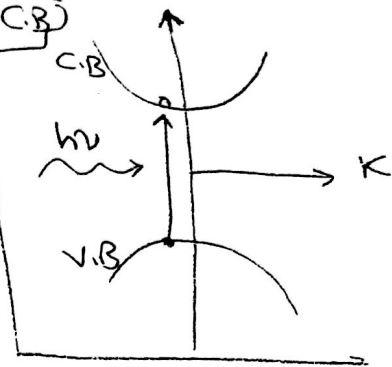
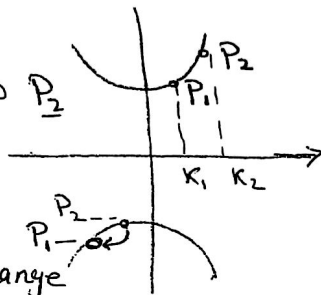
* Effects of Absorption

1] Inter band transition (Band-to-Band transition)

Electron excited From (V.B \rightarrow C.B)

2] Intra band transition (Within the Band)

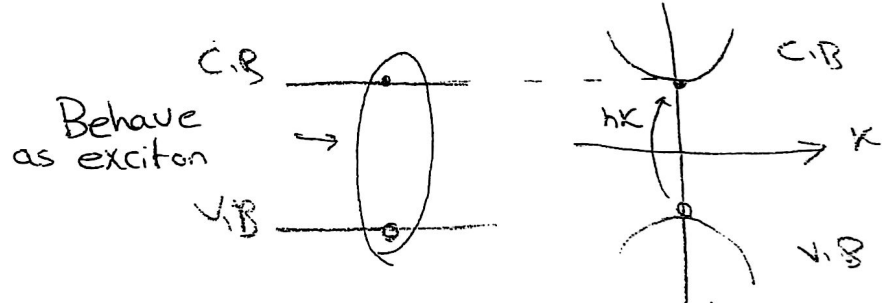
Electron in position P_1
~~make~~ make transition to P_2
 (this will require
 phonon assistant
 because there is change
 in momentum)



\rightarrow electron in $P_2 \rightarrow$ make transition to hole in P_1
 [means hole moved up]

3] phonon transition (0.01 eV \rightarrow 0.1 eV)

4] Excitonic transition: excited Electron hole pair



if i excited Electron From V.B \rightarrow C.B

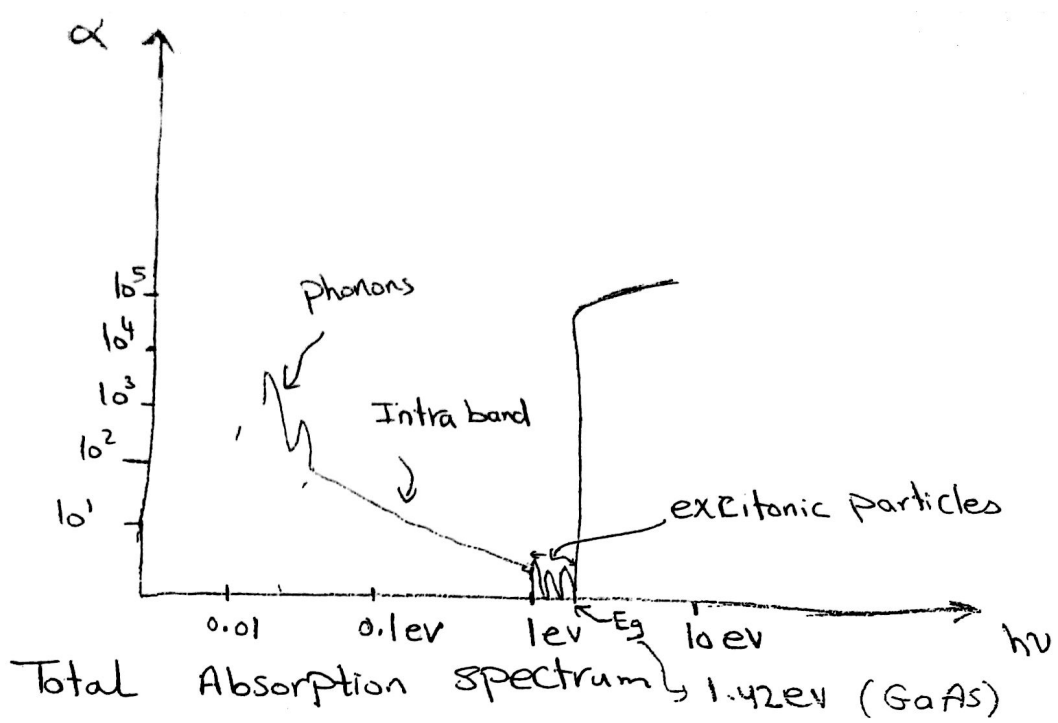
+ve charge will be in edge of V.B

-ve charge will be in edge of C.B

So, there will be Coulomb attraction between them (if they are close in space)
 (Binding energy)

Energy between electron-hole $\approx 10 \text{ meV}$

at Room temp. \rightarrow you can't see exciton because $kT = 25 \text{ meV}$



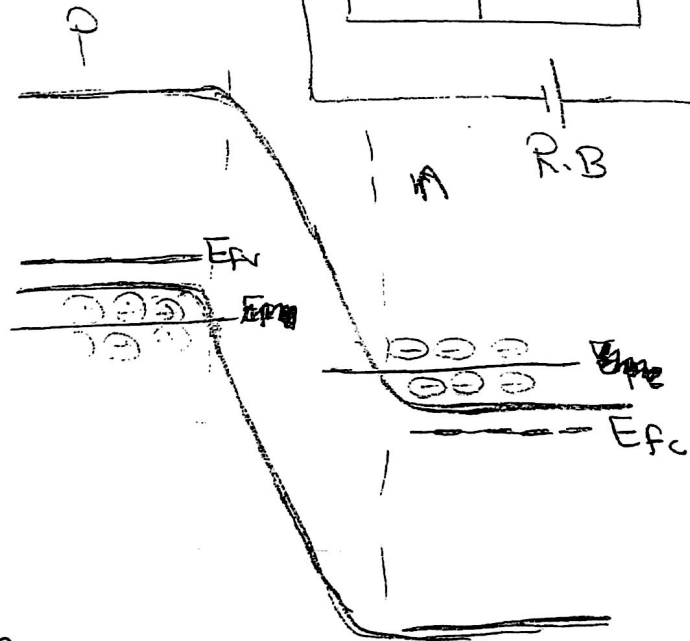
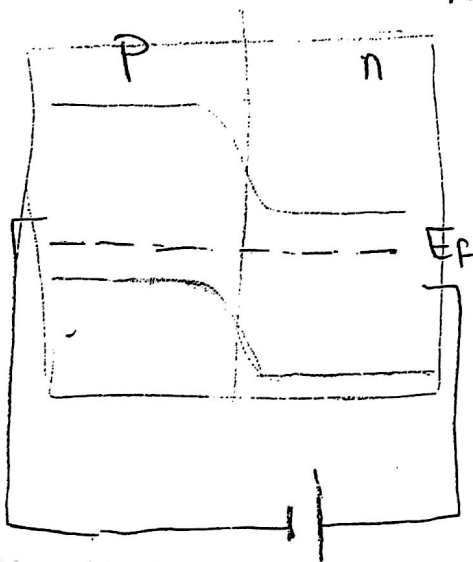
Sheet ④

Q (6)

Function of Device

① ~~Attenuator~~ Absorber (photodetector)

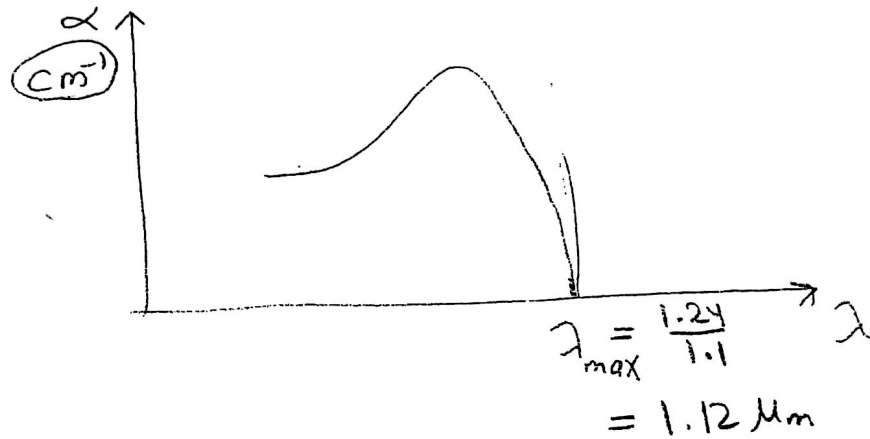
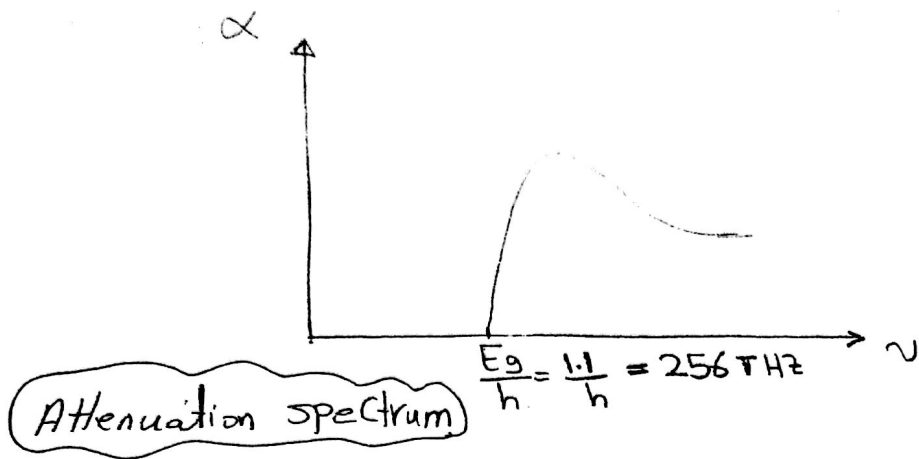
P, N \rightarrow Silicon



PN-Junction with R.B :

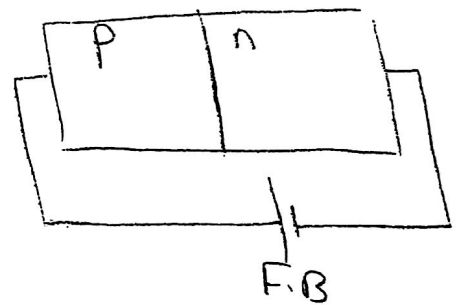
$$E_{FV} > E_{FC}$$

$$\hookrightarrow \infty \rightarrow -ve$$

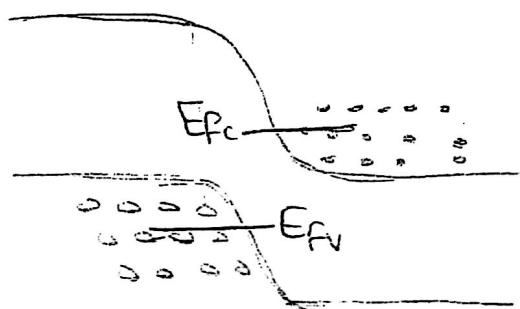


② Device function \Rightarrow LED (light source)
 \hookrightarrow Condition $P_e > P_{\text{abs}}$
 $E_{fc} > E_{fv}$

$P, n \rightarrow \text{GaAs}$



\hookrightarrow Band Diagram



Spontaneous emission spectrum:

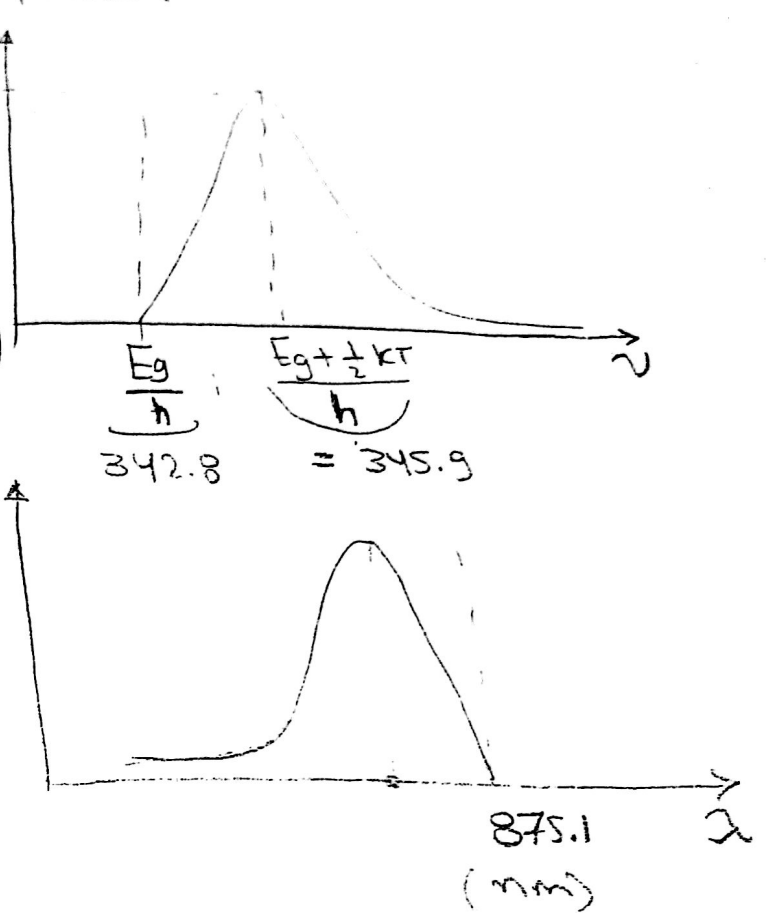
GaAs ϵ_{GaAs}

$$\nu_{\min} = \frac{E_g}{h} = \frac{1.42}{h} = 342.8 \text{ THz}$$

$$\nu_{\text{peak}} = 345.9 \text{ THz}$$

$$\lambda_{\max} = \frac{c}{\nu_{\min}} = 875.1 \text{ nm}$$

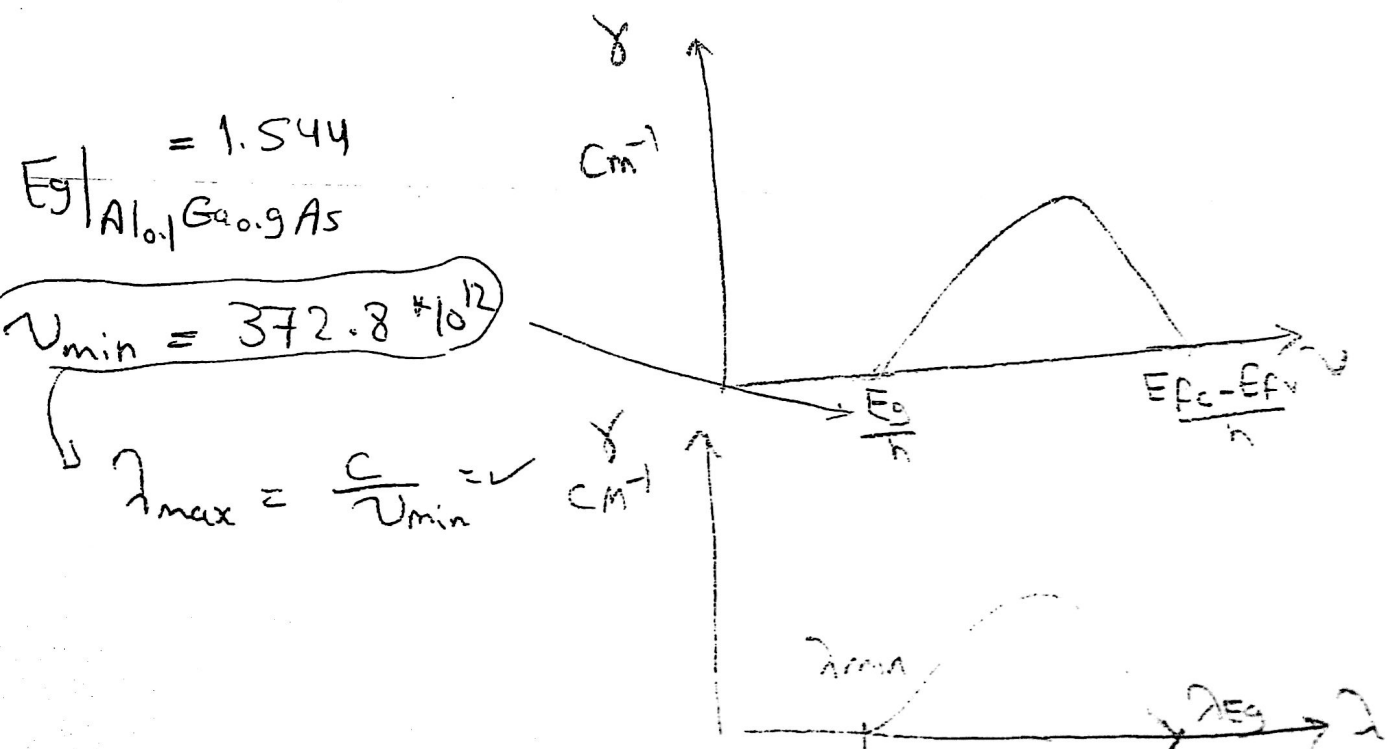
$$\lambda_{\text{peak}} = 867.3 \text{ nm}$$



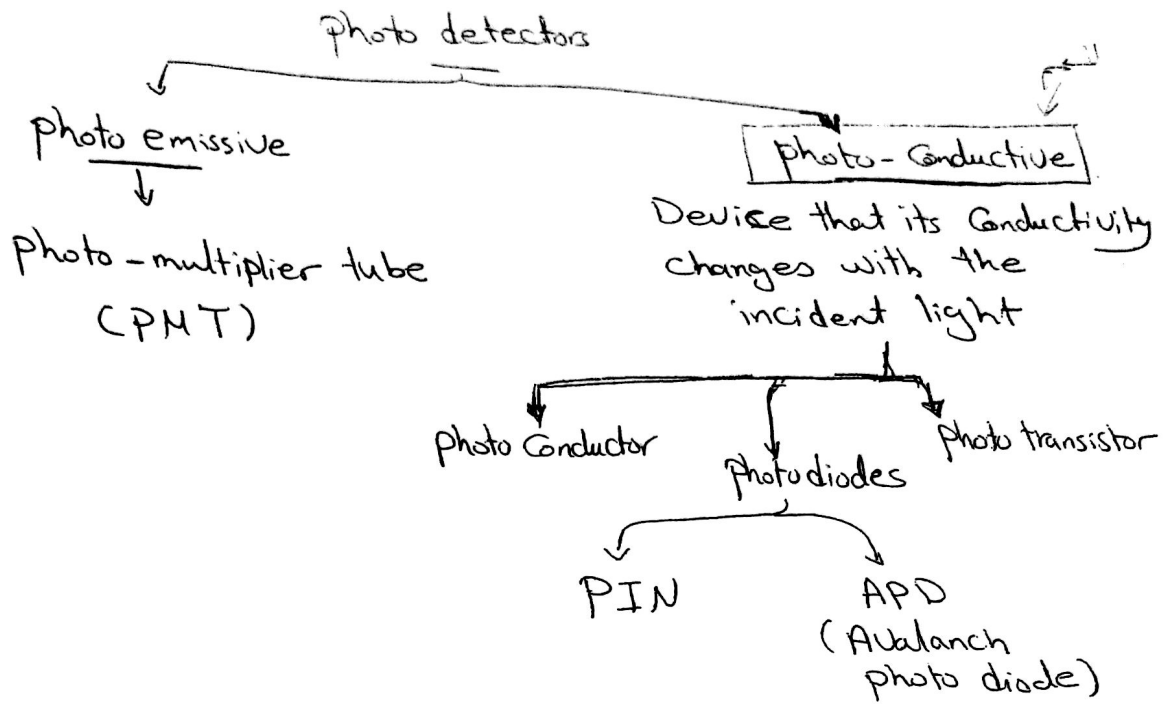
③ → Amplifier

* Band Diagram at Page (9)

+ Draw the spectra (Amp. Gain)



⑤

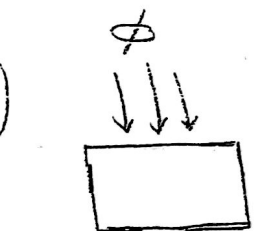


General characteristic of photodetectors :

- 1) $\eta \rightarrow$ the Quantum efficiency.
- 2) $R \rightarrow$ Responsivity.
- 3) $t_r \rightarrow$ Rise time / Impulse response (photo detector B.W. \rightarrow $\frac{1}{2\pi t_r}$)
- 4) $P_{noise} \rightarrow$ Noise power / dark Current

1) The Quantum efficiency : $\eta = \frac{\text{Carrier flux Generated which contribute to the photo current}}{\text{Incident Photon Flux}}$

$$\eta = \frac{I_p / e}{P / h\nu} = \frac{I_{ph}}{P_{opt}} \cdot \frac{h\nu}{e}$$



$$\begin{aligned} \phi &= \text{photon flux} \\ &= \frac{P_{opt}}{h\nu} \\ &= \text{No. of photons per unit time} \end{aligned}$$

2] Responsivity :

$$R_{\text{photodetector}} = \frac{i}{P_{\text{opt}}} \quad \text{A/W}$$

tell me → How much current will be generated if i pass P_{opt} (optical power).

$$\eta = \frac{i}{P_{\text{opt}}} \cdot \frac{h\nu}{e\lambda} = R_{\text{det.}} \cdot \frac{1.24}{\lambda (\mu\text{m})}$$

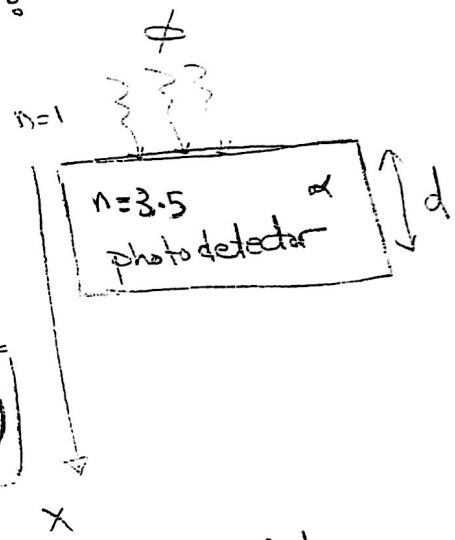
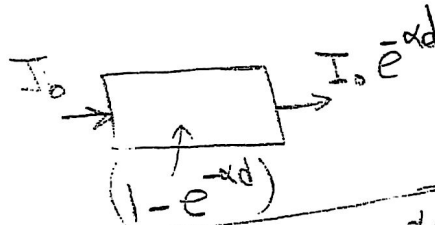
$$R_{\text{det.}} = \eta \cdot \frac{\lambda (\mu\text{m})}{1.24}$$

$$R \propto \eta$$

(if you want to maximize R you want $\eta \rightarrow \text{max.}$)

→ To increase R ⇒ we need to increase η :

① what is η ?



$$\text{Fractional no. of photons absorbed} = \phi (1-R) (1-e^{-\alpha d})$$

① ليس كل ال photons

النافذ في سطح Current

يمكن صنع phonons

② يمكن ال electron

- hole

الناتج يحدث بينا recombine

ولا في Current

نتيجة اختلاف ال n في جزء من ال power هينعكس

في فالقيمة اللى هتدخل ال Detector $(1-R_{\text{ref}})\phi$

$R_{\text{ref}} \Rightarrow$ refractivity

$$0 < \tau < 1$$

$N \rightarrow$ No. of Absorbed Photons
 $\tau \cdot N \rightarrow$ no. of photons generate current

$$\therefore \text{Energy Absorbed} = \phi (1 - R_{\text{ref}}) (1 - e^{-\alpha d}) \tau$$

$$\therefore \eta = \frac{\phi (1 - R_{\text{ref}}) (1 - e^{-\alpha d}) \tau}{\phi}$$

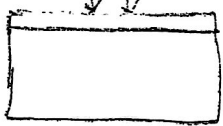
$$\eta = (1 - R_{\text{ref}}) (1 - e^{-\alpha d}) \tau$$

To $\eta \gg$

① R_{ref} make it ≈ 0

How?

By using (Anti Reflection Coating)



$$e^{-\alpha d} \approx 0$$

\hookrightarrow We need to make (αd) to be large

$$\tau \approx 1$$

$d \rightarrow$ maximize Thickness of PD

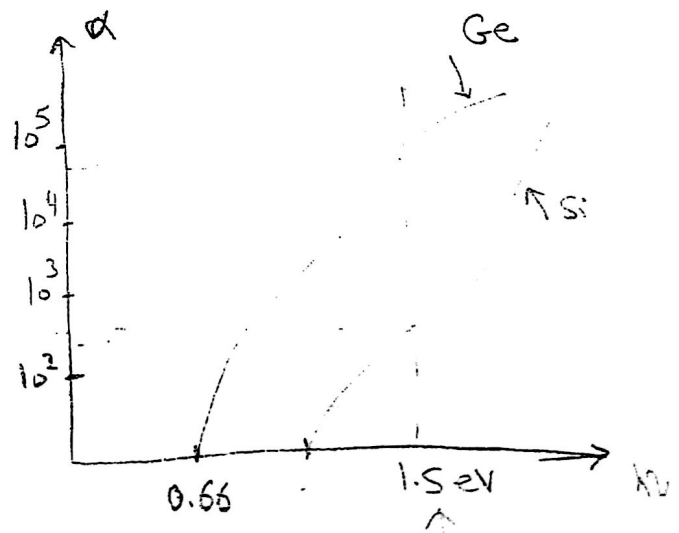
$d \uparrow$

\rightarrow How to maximize α ?

$$\alpha_{\text{Ge}} > \alpha_{\text{Si}}$$

\hookrightarrow When i use the same light source

\rightarrow Then i can use Ge



ALGaAs / GaAs Laser

Note

Thickness of photo detector depend on α

Ex: IF i need 90% of light to be Absorbed

$$\therefore (1 - e^{-\alpha d}) = 0.9$$

$$e^{-\alpha d} = 0.1 \Rightarrow -\alpha d = \ln(0.1)$$

$$\boxed{d = \frac{1}{\alpha} \ln(10)}$$

if i use $\alpha = 20,000 \text{ cm}^{-1}$ (Ge)

$$\therefore d = \frac{1}{20,000} \times 2.303 = 0.115 \times 10^{-3} \text{ cm} \\ = \underline{\underline{1.15 \mu\text{m}}}$$

③ \rightarrow how to maximize ?

\uparrow
no. of Absorbed photons that generate current

By very ~~careful~~ ^{Careful} fabrication of the detector material.

"To make less defects \rightarrow less trap states"
electron hole recombination \downarrow

Q(8)

Give reason for:

g) Coating the top of sensor by thin transparent layer.

→ To minimize the reflectivity (R_{ref})

Then η will increase

$$\text{as } \eta = (1 - R_{ref})(1 - e^{-\alpha d}) \approx$$

So → The responsivity will increase

$$R = \eta \cdot \frac{\lambda \text{ (nm)}}{1.24}$$

[Current generated will increase]

h) Sensor made from Ge is thinner than that made of Si with identical Quantum eff.

$$\rightarrow \eta = (1 - R_{ref})(1 - e^{-\alpha d}) \approx$$

$$\alpha_{Si} < \alpha_{Ge} \Rightarrow d_{Si} > d_{Ge}$$

$$\text{Page (3)} \leftarrow \frac{(q h \nu_s (h \nu))}{(h \nu_s)} +$$

Mansoura University	Faculty of Engineering	Electronics and Comm. Dept.	4 th Year, Optical Communication Systems	16/12/2015	Updated Sheet #4
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Q₁) Complete the following sentences with suitable word(s):

- In dense wavelength division multiplexing, the separation between successive wavelength is equal to
- Double hetero structure is defined as.....
- The Thickness of active material in double heterostructure should be less than.....
- The deBroglie wavelength at $T=300K$ for GaAs with $m^*=0.067m_0$ is equal to.....
- At thermal equilibrium, the probability of emission is..... than the probability of absorption.
- The energy of phonons lies within the range
- The momentum of electron is that of phonon.
- The momentum of electron is that of photon.
- The phonon has energy and momentum.
- The photon has energy and momentum.
- Absorption of energy with generates phonons.
- Absorption of energy (Eg-10mev) generates.....

Q₂) Compare between:

- Photon and Phonon.
- Optical Phonon and acoustic Phonon.
- Radiative transition Non-Radiative transition.
- Photon assisted transition and phonon assisted transition.
- Structure $Al_{0.1}Ga_{0.9}As/GaAs / Al_{0.1}Ga_{0.9}As$, thickness of GaAs=15 nm and $Al_{0.1}Ga_{0.9}As/GaAs / Al_{0.1}Ga_{0.9}As$, thickness of GaAs=12 nm.
- The spontaneous emission, stimulated emission, absorption with the aid of (E-K) diagram & applications.
- Irradiance, Energy density and Flux
- Amplifier and attenuation using E-K diagram at $T=0K$. \rightarrow Sec (9) Page (3)
- Interband transition & Intraband transition.
- Amplification gain coefficient at $T=0K$ and $T=300K$.
- Quantum efficiency and responsivity
- Carrier transit time and carrier recombination time
- Sensitivity, dynamic range and linearity of the detector

Q₃-Draw the following curves:

- Rate of spontaneous emission for $Ga_{0.9}Al_{0.1}As$ & $Al_{0.2}Ga_{0.9}As$ at $T=300K$
- Rate of spontaneous emission for $Ga_{0.9}Al_{0.1}As$ at $T=300K$ & $T=200K$ & $T=400K$
- Typical attenuation curves for Si, Ge, GaAs, GaN
- Responsivity vs. wavelength for Si and InGaAs

Q4) Given $\text{Al}_{0.2}\text{Ga}_{0.8}\text{As}/\text{GaAs}/\text{Al}_{0.2}\text{Ga}_{0.8}\text{As}$

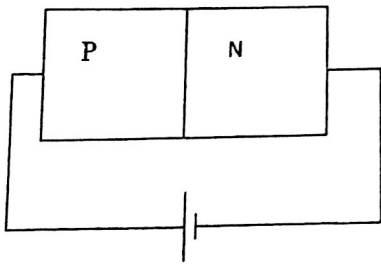
- Draw the structure, defining (determine) the available thickness for GaAs layer
- Draw the band diagram for the structure qualitatively.
- Explain the operation of the structure with the aid of (b) and determine the application that this device can be used for.
- Determine the maximum and minimum emitted wavelengths.

Q5) Estimate the following relation

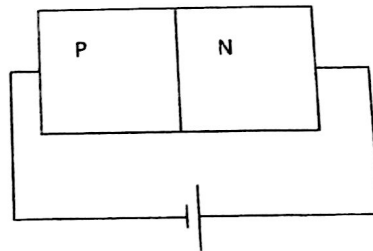
- Optical Joint of state $\rho_{c,v}(v)$.
- Rate of spontaneous emission.
- The probability of emission and absorption at thermal equilibrium.
- The probabilities of emission and absorption at quasi thermal equilibrium.
- K-selection rule.
- Amplification gain in stimulated emission
- Conditions for amplification (stimulated emission)

Q6) Given

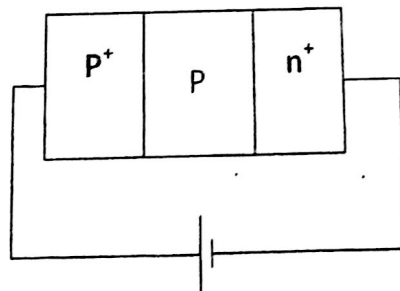
P layer and N layer are made of Ga As



P layer and N layer are made of Si



$\text{P}^+ : \text{Al}_{0.1}\text{Ga}_{0.9}\text{As}$, $\text{P} : \text{GaAs}$, $\text{n}^+ : \text{Al}_{0.1}\text{Ga}_{0.9}\text{As}$



- Draw the band diagram for each structure
- Explain the operation and define the function of each device.

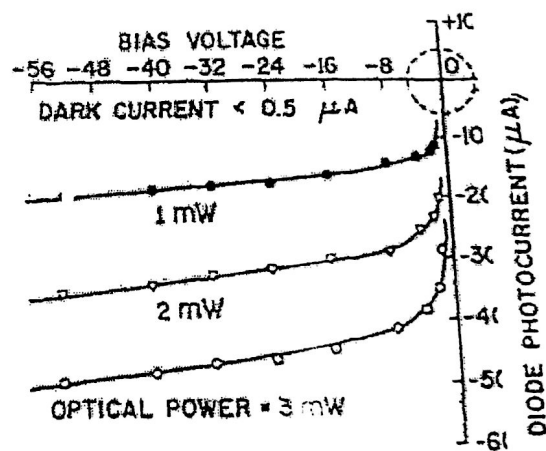
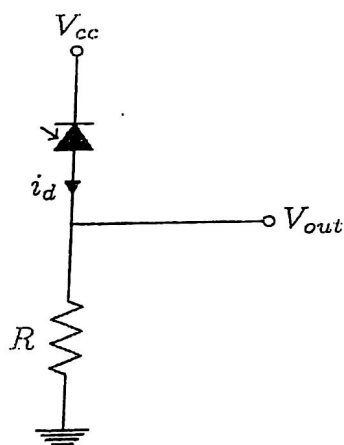
- a) Draw the load line of the circuit, the output voltage vs. the incident power
- b) Calculate the dynamic range and how to increase the dynamic range
- c) Calculate the sensitivity and how to increase the sensitivity
- d) Calculate the output noise power and how to decrease it.
- c) Draw the variations of the spectra (spontaneous emission, attenuation constant and amplification gain) of each device vs.
- ν (Frequency)
 - λ (wavelength)

Q7) Given semiconductor amplifier $\text{In}_{1-x}\text{Ga}_x\text{As}_{1-y}\text{P}_y$ with $E_g = 1.12 \text{ eV}$ & peak gain coefficient $= 60 \text{ cm}^{-1}$ and B.W $= 300 \text{ nm}$, draw the variation of gain coefficient vs. ν (Frequency) and λ (wavelength)

Q8. Give reason for

- Si absorbs photon with energy $< 1.1 \text{ eV}$
- The width of P-layer in PN junction detector is less than N-layer
- InGaAs is preferred for designing fast response detector
- Ge is not preferred for designing sensitive detector
- Si is preferred for designing solar cells
- Quantum well structures are suitable for DWDM
- Coating the top of sensor by thin transparent conductive layer
- Sensor made from Ge is thinner than that made of Si with identical quantum efficiencies
- Purified materials are necessary for designing sensor with good responsivity
- Si is used sensor within the wavelength range 300 nm up to 1100 nm only

Q9. Given the circuit below, with $V_{cc} = 24 \text{ volt}$, $R = 12 \text{ M}\Omega$



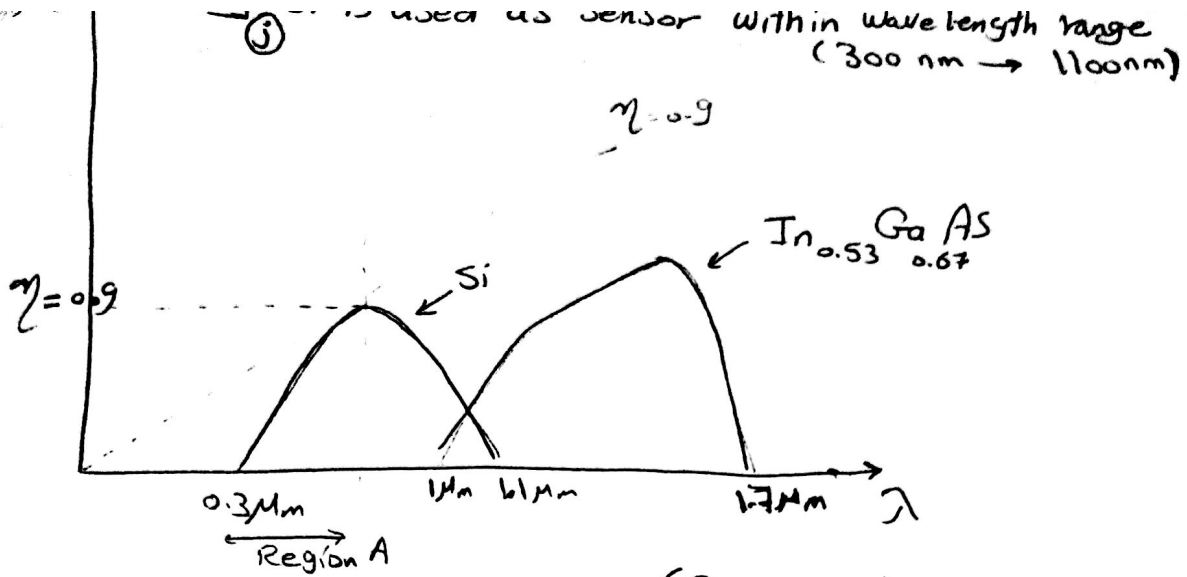
- Draw the load line of the circuit, the output voltage vs. the incident power
- Calculate the dynamic range and how to increase the dynamic range
- Calculate the sensitivity and how to increase the sensitivity
- Calculate the output noise power and how to decrease it.

Q10. Explain the function, advantage of the PIN diode and give practical design.

رابعة اتصالات

مقرر OPTICS

part (١٥)



\hookrightarrow Silicon has $E_g = 1.1 \text{ eV}$ ($\lambda_g = 1.1 \mu\text{m}$)

\hookrightarrow photons have energy $> 1.1 \text{ eV}$

Si must absorb them and generate current ($\eta \gg$ for $\lambda < 1.1 \mu\text{m}$)

\hookrightarrow η goes down in (A) Region:

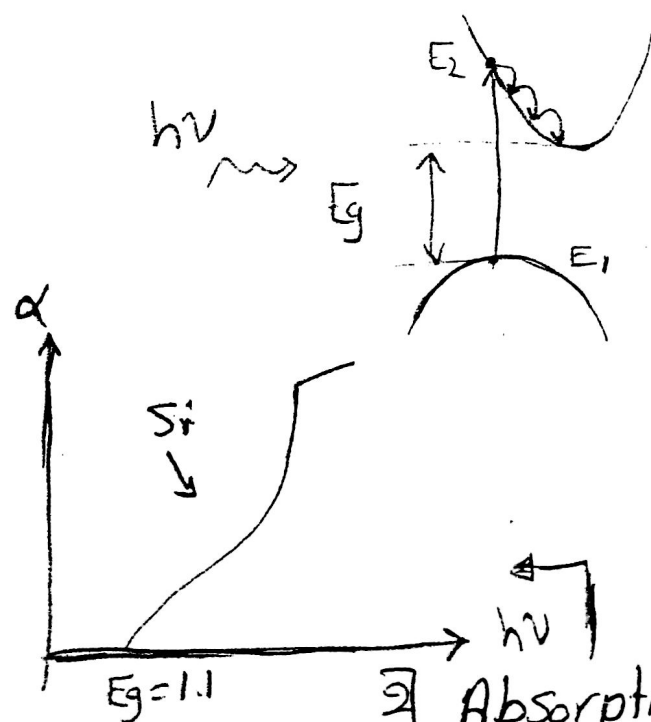
1] Generation of hot Carriers

When $h\nu > E_g$

electron Jumps from $E_1 \rightarrow E_2$

This electron called hot electron because it loss energy Through Thermalization (Generate phonon)

\rightarrow So reCombination take place Very Quickly



2] Absorption near the surface (reCombination Cause of trap State) for $h\nu > E_g$ \Rightarrow $\alpha \rightarrow$ will be large

Then $d \rightarrow$ will be small

because ($e^{-\alpha d}$)

Note

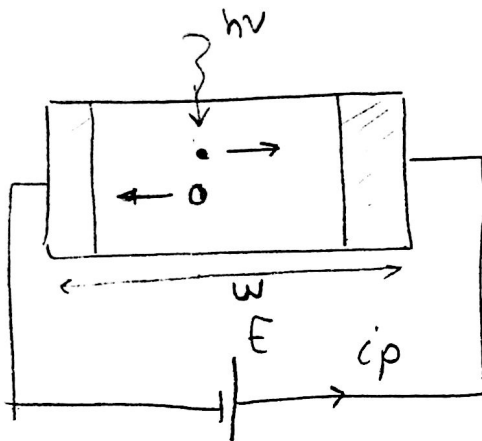
① At $1.55 \mu\text{m}$ (Fiber Application)

↳ In GaAs is commonly used

② For Solar cell at $(0.3 \mu\text{m} \rightarrow 0.8 \mu\text{m})$

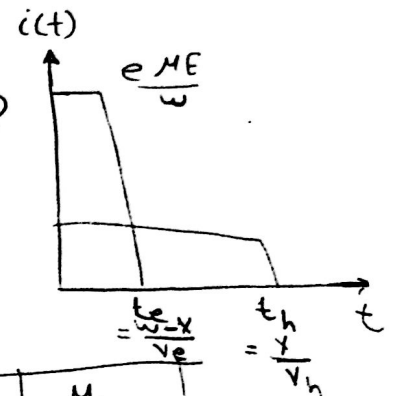
↳ Silicon is commonly used detector

③ Response time (How fast the detector is?)



$$i(t) = - \frac{q \nu(t)}{w}$$

$$\nu(t) = ME$$



Material	M_e	M_h
Si	1500	450
In Ga As	14,000	400

↳ To increase the speed of detector?

1] Choose material with high mobility.
(Ex : In Ga As)

2] Reduce the dimensions of detector
(Active layer)

3] Apply Electric field to help Carriers
to move fast.

③ In GaAs is preferred for designing fast response detector

① Because it has large values of μ_e , μ_h and $V_{sat} = 10^7$ (very sharp impulse response)

بالنسبة لـ GaAs، فإن سرعة الإلكترونات عالية جداً، مما يجعلها مناسبة للاستجابة السريعة.

→ Note

Impulse Response depend on 2-factors

transit time

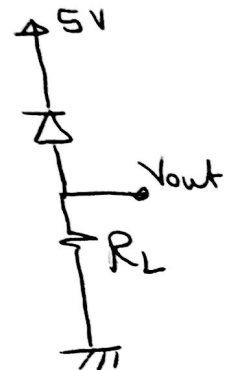
$$t_e = \frac{w}{\mu E}$$

→ To minimize it

- * increase μ and E
- * decrease w

(دو إلى التقليل في التوقيتات)

Time Constant of the Circuit



$$\tau = R_L \cdot C$$

↑
Junction Cap.

$$f = \frac{1}{2\pi R_L C}$$

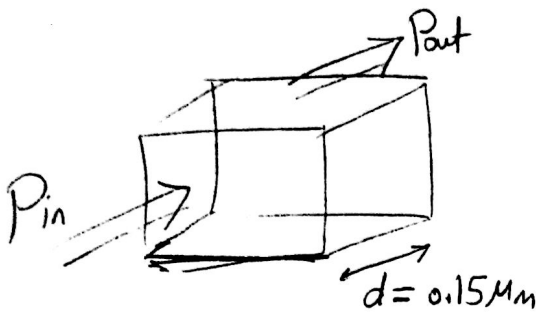
At Detector Data sheet

$$\tau = 0.3 \text{ ns} \rightarrow \text{at } R_L = 50 \Omega$$

Ex 8 Given PIN photodiode made of $\text{InGaAs}_{0.53\ 0.47}$

- a) if the Thickness of I-layer = $0.15\ \mu\text{m}$
and Absorption Coeff. $\alpha = 1.5\ \mu\text{m}^{-1}$ at $\lambda = 1300\ \text{nm}$
→ Determine the percentage of Absorbed photons by PIN diode.

or
w/



$$P_{out} = P_{in} e^{-\alpha d}$$

$$= P_{in} (e^{-(0.15 \times 1.5)})$$

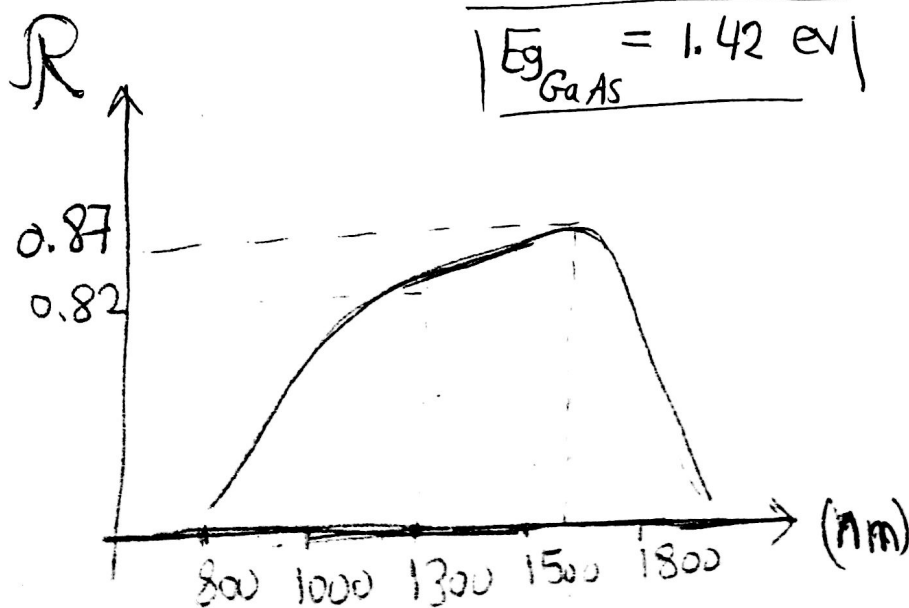
$$\approx 0.8 P_{in}$$

$$\therefore P_{absorbed} = \frac{P_{in} - 0.8 P_{in}}{P_{in}} \times 100$$

$$P_{abs} = 20\%$$

b) Given Responsivity Curve for $\text{InGaAs}_{0.53\ 0.47}$

- i) Determine the Band Gap?
ii) Determine the incident optical power to generate $I_{ph} = 10\ \text{nA}$ at $\lambda = 1.55\ \mu\text{m}$
iii) Will the PIN Detector detect the maximum emitted λ from Laser diode made of GaAs?



$$|E_{g_{GaAs}} = 1.42\ \text{eV}|$$

(2)

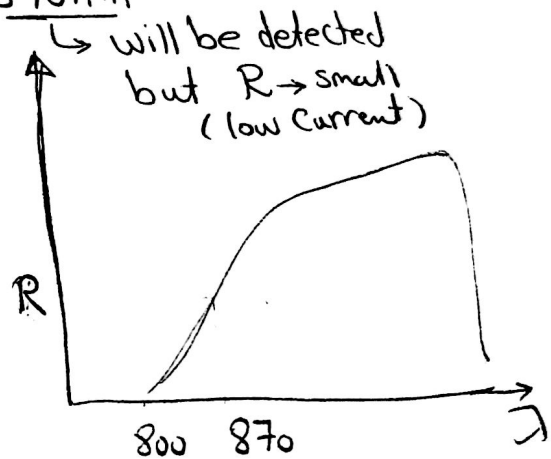
Sol i) $\lambda_g = 1800 \text{ nm} \rightarrow E_g = \frac{1.24}{\lambda_g(\mu\text{m})} = \frac{1.24}{1.8} = 0.69 \text{ eV}$

ii) $R = \frac{i_{ph}}{P_{opt}} \Rightarrow$ ^{From curve} at $\lambda = 1.55 \mu\text{m} \Rightarrow R = 0.87$

$P_{opt} = \frac{i_{ph}}{R} = \frac{10 \text{ nA}}{0.87} = 11.5 \text{ nW}$ w/

iii) GaAs $\rightarrow E_g = 1.42 \text{ eV}$

$\lambda_g = \frac{1.24}{1.42} = 870 \text{ nm}$



Note Dark Current :

The reverse current when there is no incident photons

Typical values :

Si $\sim 1 \text{ nA}$

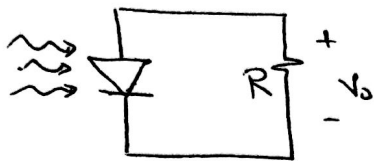
Ge $\sim 200 \text{ nA}$

InGaAs $\sim 100 \text{ nA}$

photo diodes

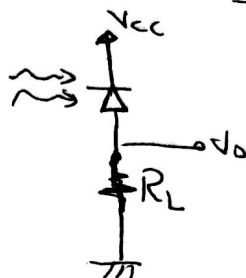
I Two modes of operations

I Photo Voltaic



- * No Reverse Bias Applied
- * Slower Device

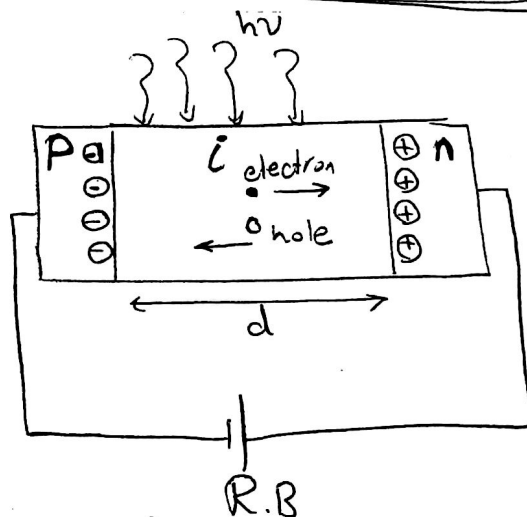
II photoConductive



- * Apply Reverse Bias
- * More Conductive
- * high Responsivity
- * Speed device

PIN Diode

(positive intrinsic Negative)



Introduction the intrinsic Region :

- * Increase area of capturing light (large η)

* $C = \frac{\epsilon A}{d}$, $d \rightarrow$ is large $\Rightarrow C$ is small \Rightarrow Fast Response

$$R = \frac{1}{2\pi R_L C}$$

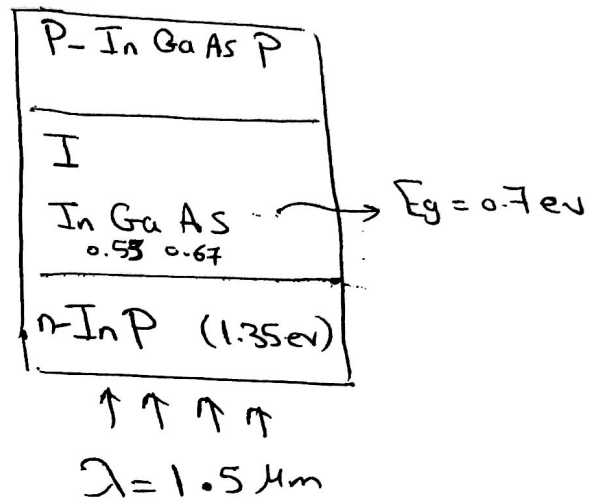
→ Practical PIN Design :

0
7/11

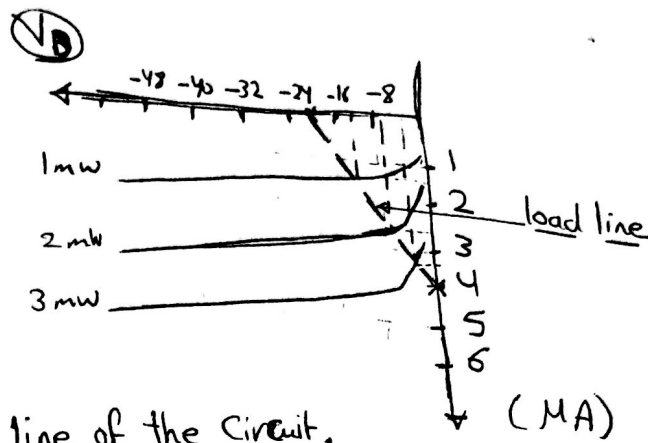
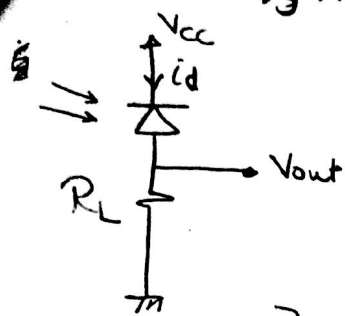
InP $\rightarrow E_g = 1.35 \text{ eV}$
and incident $\lambda = 1.5 \mu\text{m}$
(0.7 eV)

So, this layer works as
transparent material

$$E_g > E_{g|\text{incident}}$$



Given the Circuit below,
with $V_{CC} = 20$ Volt
 $R = 15$ M Ω



- Draw the load line of the circuit, the o/p Voltage Vs. the incident power
- Calculate the dynamic Range and how to increase the dynamic range.
- Calculate the Sensitivity and how to increase it.
- Calculate the o/p noise power and how to decrease it.

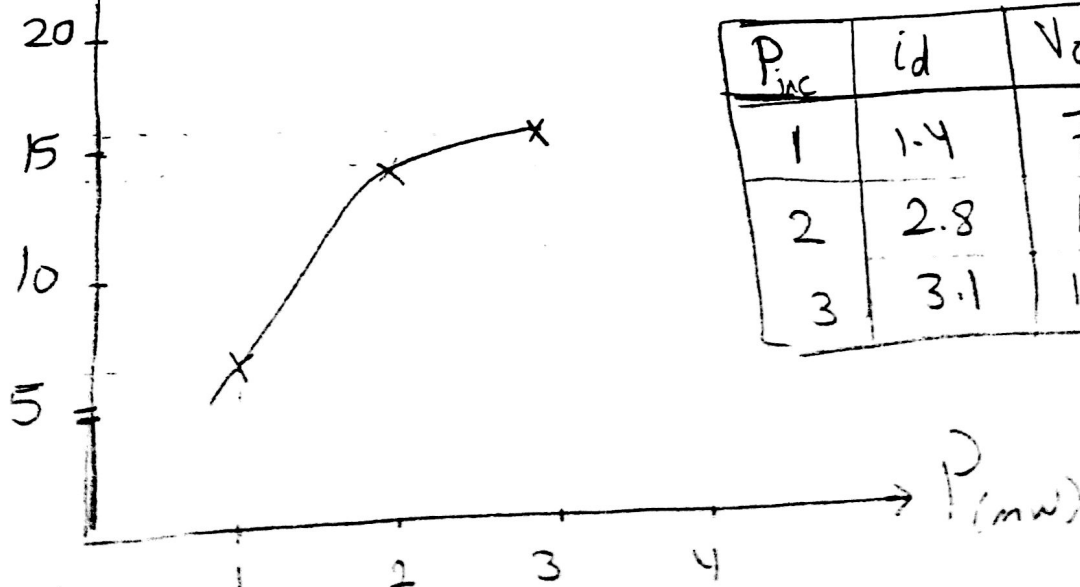
Prob load line : $V_{CC} + V_d + i_d R_L = 0$

$$i_d = -\frac{V_{CC}}{R_L} - \frac{V_d}{R_L}$$

at $i_d = 0 \rightarrow V_d = -20$

at $V_d = 0 \rightarrow i_d = 4$ mA

$$V_o = i_d R_L$$



P_{inc}	i_d	$V_o = i_d \cdot R_L$
1	1.4	7
2	2.8	14
3	3.1	15.5

$$b) \text{ Dynamic Range} = \frac{\text{max power}}{\text{min power}} \text{ dB}$$

$$= 10 \log \frac{15.5 \times 10^{-3}}{7 \times 10^{-3}} = 3.4 \text{ dB}$$

10
10

↳ To increase Dynamic Range → Decrease load Resistance

c) Sensitivity (min. power generate current)

$$S = 1 \text{ mW}$$

↳ To increase Sensitivity → use large R_L

d) Noise power

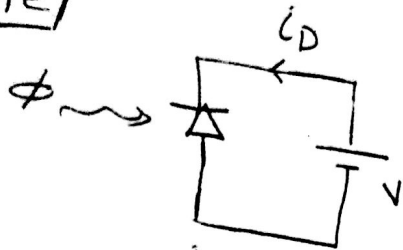
given
↳ Dark Current $\leq 0.5 \mu\text{A}$

$$P_{\text{noise}} = (i_d)^2 R_L = (0.5 \times 10^{-6})^2 \cdot 5 \times 10^6$$

$$= 1.25 \mu\text{watt}$$

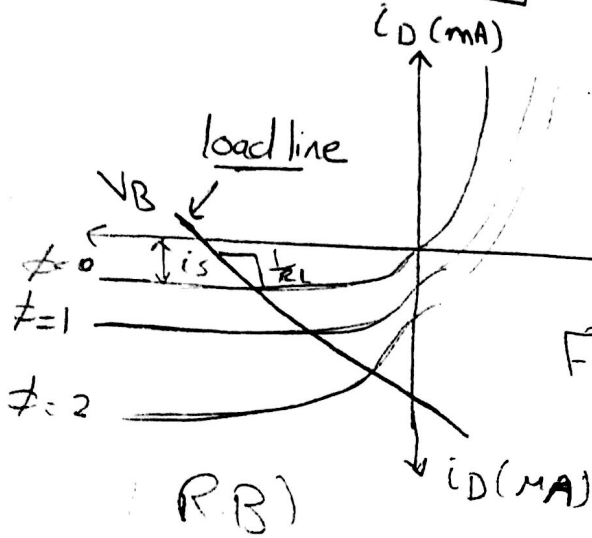
↳ To decrease Noise power:
↳ decrease load Resistance

Note



$$i_D = i_s (e^{\frac{eV}{kT}} - 1) - i_p$$

Photo Generated Current

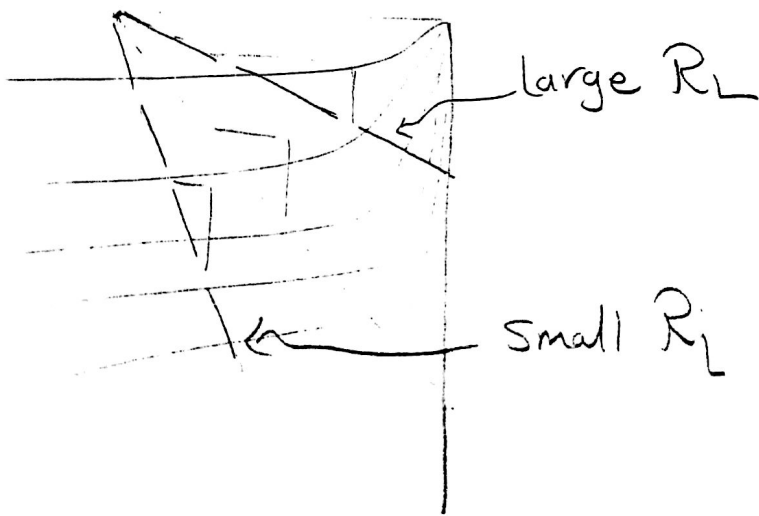


$$V_B = V_d + i_D R_L = 0$$

$$i_D = -\frac{1}{R_L} V_d - \frac{V_B}{R_L}$$

Const.

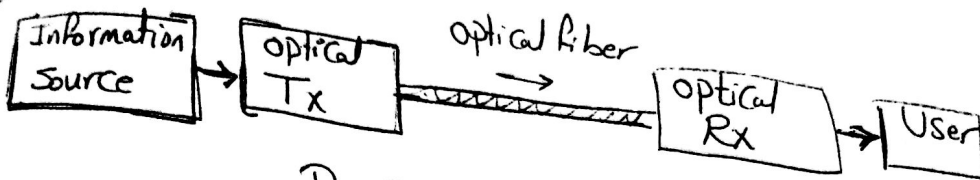
للمصدر $V_B = \text{Const.}$
مقاومة الحمل $R_L = \text{Const.}$



حدد النقاط التي سيتقاطع فيها ال load line مع ال Curve لتزيد

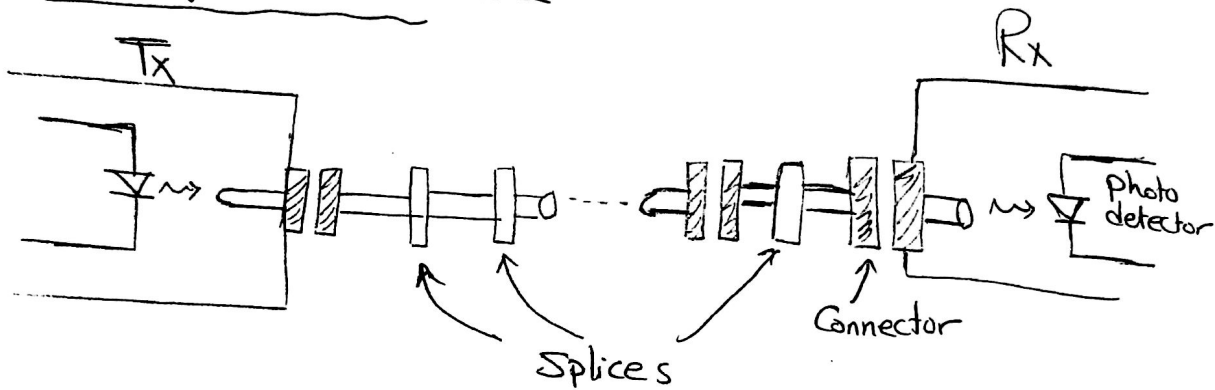
يعتبر ال Dynamic Range

Fiber link Design:



① Simple point-to-point link

② Optical Power loss-model



Connectors → ① Connect fiber to Rx and Tx Blocks
② Testing and measuring purposes.

Splices → permanent Connection

↳ To design fiber link :

- ① The length of link (Km)
- ② Bit rate (Mb/s)
- ③ Bit error rate

④ select Source :

LED → 100 μwatt

Laser diode → 1mw → 0dBm

$$= 10 \log \frac{10^{-3}}{10^{-3}} = 0$$

Power Budget Calculations :

P_s = Power from transmitter in dBm

P_r = Sensitivity of Rx in dBm from given BER

Max. allowable loss $[\alpha_{max} = P_s - P_r]$

$$\alpha_{max} = \alpha_{fiber} + \alpha_{connectors} + \alpha_{splice} + \alpha_{sys.}$$

$$\alpha_{fiber} = \alpha_{max} - [\alpha_{Conn.} + \alpha_{splice} + \alpha_{sys.}]$$

↑
Safety Margin
6dB

$$\text{Power limited link length} = \frac{\alpha_{fiber}}{\text{loss/km}}$$

→ Beyond this distance the SNR is below the Acceptable limit.

Rise time Budget

Rise time analysis gives effective B.W of link:

$$t_{sys} = \sqrt{t_{Tx}^2 + D^2 \sigma_\lambda^2 L^2 + t_{Rx}^2}$$

for satisfactory operation of the link

$$t_{sys} \leq 0.7 T_b$$

$\sigma_\lambda \rightarrow$ Spectral width of optical source

$D \rightarrow$ material dispersion

$T_b \rightarrow$ pulse duration

Link Power Budget:

is an accounting procedure in which one calculates how much power can be lost between T_x and R_x for given receiver sensitivity (which depends on bit rate)

Rise time Budget : is an accounting procedure in which one calculates how much pulse spreading can be tolerated between T_x and R_x for a given T_x rise time, ~~receiver~~ receiver rise time and dispersion due to fibre.

Ex:



$\sigma_\lambda = 0.1 \text{ nm}$, $P_{Tx} = -8 \text{ dB}$

$P_{Rx} = -34 \text{ dB}$

$D = 5 \text{ ps / km / nm}$

- 5 Splice \rightarrow each has loss = 0.1 dB/km
- 2 Connector \rightarrow " " " = 0.75 dB/km
- $\alpha = 0.2 \text{ dB/km}$ at $\lambda = 1550 \text{ nm}$

\hookrightarrow Calculate link length?

\hookrightarrow Calculate Rise time?

SOL~

$\alpha_{\text{max}} = P_t - P_r = -8 - (-34) = 26 \text{ dB}$

$\alpha_{\text{Connector}} = 2 * 0.75$

$\alpha_{\text{splice}} = 5 * 0.1$

Safety Margin

$\therefore L = \frac{26 - [(2 * 0.75) + (5 * 0.1) + 6 \text{ dB}]}{0.2}$

$L = 90 \text{ km}$

\hookrightarrow you ~~will~~ won't need ~~Repeater~~ AMP Repeater for $L < 90 \text{ km}$
SNR \rightarrow acceptable

السرعة
المطلوبة
90 كم
السرعة
المطلوبة
2*10³ كم

$t_{\text{Disp.}} = D \cdot \sigma_\lambda \cdot L_{\text{RTmax}}$

$T_b = 10^{-9}$, $D = 5 \text{ ps / km / nm}$, $\sigma_\lambda = 0.1 \text{ nm}$

$L_{\text{RTmax}} = \frac{10^{-9}}{0.15 * 10^{-12}} = 2 * 10^3 \text{ km}$

Signal Can travel without distortion to $2 * 10^3 \text{ km}$, but SNR become unacceptable after $2 * 10^3 \text{ km}$